

# AFFINE TRANSLATION SURFACES WITH $\Delta^{\Pi} \mathbf{r}_i = \lambda_i \mathbf{r}_i$ IN THE GALILEAN 3-SPACE

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**Abstract**—A translation surface is the space obtained by identifying pairwise by translations the sides of a collection of plane polygons. The simplest example of a translation surface is obtained by gluing the opposite sides of a parallelogram. It is a flat torus with no singularities. The translation surfaces, among the family of surfaces in classic differential geometry, have been commonly examined since early 1900s.

In this paper, we investigate the affine translation surfaces in the 3-dimensional Galilean space  $G^3$ . Further, we classify the affine translation surfaces in  $G^3$  under the condition  $\Delta^{\Pi} \mathbf{r}_i = \lambda_i \mathbf{r}_i$ , where  $\lambda_i \in \mathbb{R}$  and  $\Delta^{\Pi}$  denotes the Laplace operator with respect to the fundamental form  $\Pi$ .

**Keywords:** Galilean space; affine translation surface; Laplace operator.

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## References:

- [1] Z. M. Sipus and B. Divjak, *Translation surfaces in the Galilean space*, Glasnik Mathematicki **46**(2011) 455-469.
- [2] M. E. Aydin and M. Ergut, *Affine translation surfaces in the isotropic 3-space*, arXiv: 1611.02595v2 (2016).
- [3] H. Liu, Y. Yau, *Affine translation surfaces in Euclidean 3-space*, In: Proc. of the Japan Academy, Ser. A, Math. Sci. **89** (2013) 111-113.
- [4] M. K. Karacan, D. W. Yoon, and B. Bukcu, *Translation surfaces in the three dimensional simply isotropic space  $I_3^1$* , Int. J. Geome. Methods Mod. Phys. **3** (2016) no. 7 1650088 9 pages.